

# Theory of machine

If you have a smart project, you can say "I'm an engineer"

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## Lecture 5

Instructor

Dr. Mostafa Elsayed Abdelmonem

# Theory of machine

## MDP 234

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- **Lecture aims:**
  - Learn fundamental concepts and terminology
  - Learn how to design a cam and follower set to achieve a desired output motion.

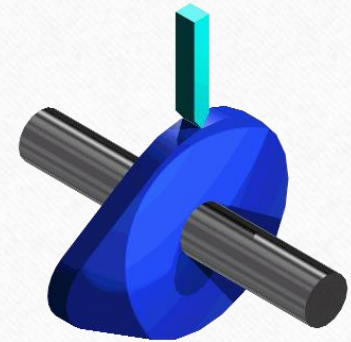


# Introduction

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## 1.1 CAM - Definition

- Cams are used to convert rotary motion into reciprocating motion.
- Necessary **elements** of a cam mechanism are
  - A **driver** member known as the *cam*
  - A **driven** member called *the follower*
  - A **frame** which supports *the cam and guides the follower*

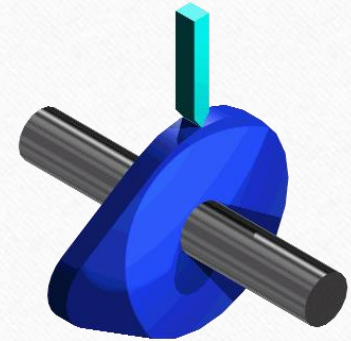


# Introduction

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## 1.1 CAM - Definition

- Cams are **widely used** in automatic machines, internal combustion engines, machine tools, printing control mechanisms, and so on.
- They are **manufactured** usually by die-casting, milling or by punch-presses.
- A cam and the follower combination belong to the category of **higher pairs**.

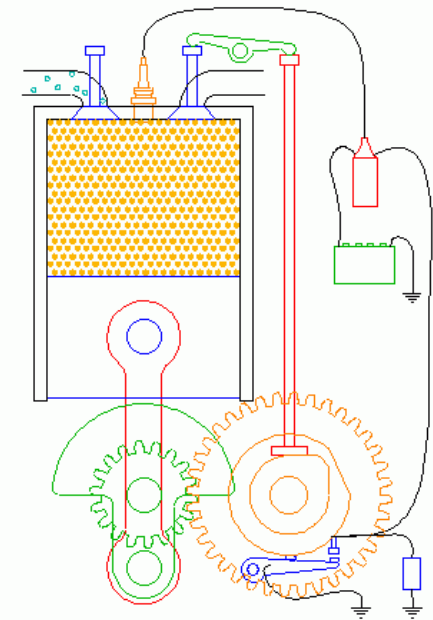
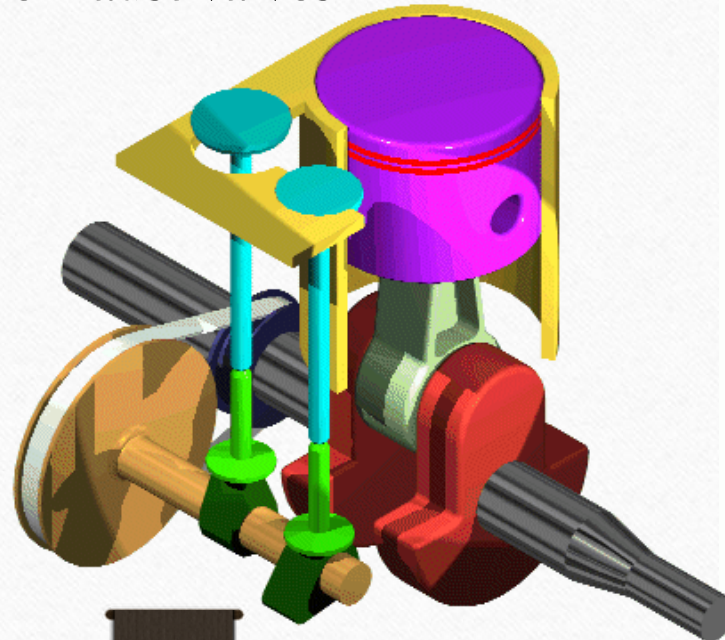




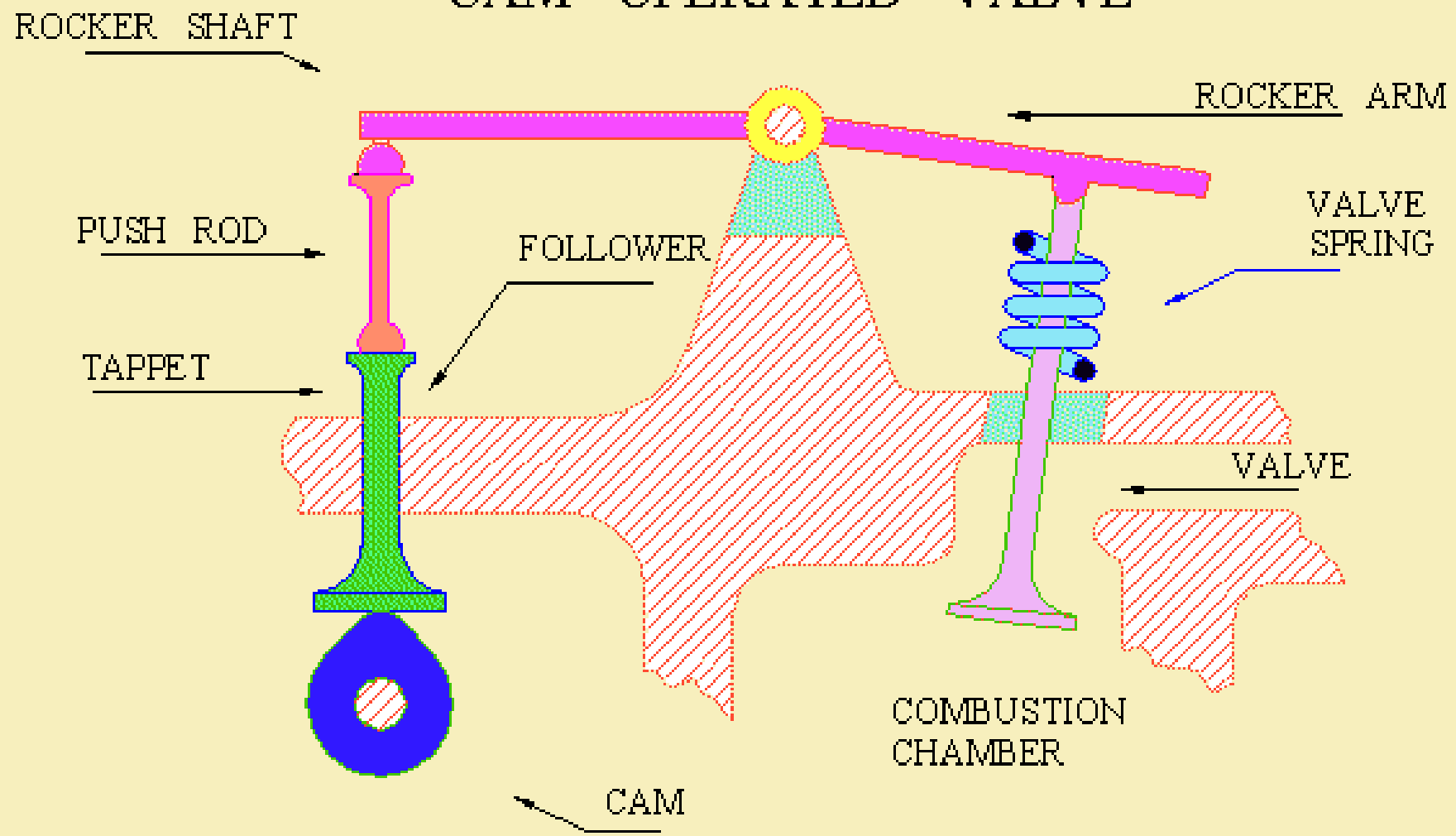
# Introduction

## Examples for cam

- In IC engines to operate the inlet and exhaust valves



# CAM OPERATED VALVE



# Cam Mechanism

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## 1.2 Classification of CAM Mechanism

### I. According to modes of Input / Output motion

1.2.1 Rotating cam – Translating follower

1.2.2 Rotating cam – Oscillating follower

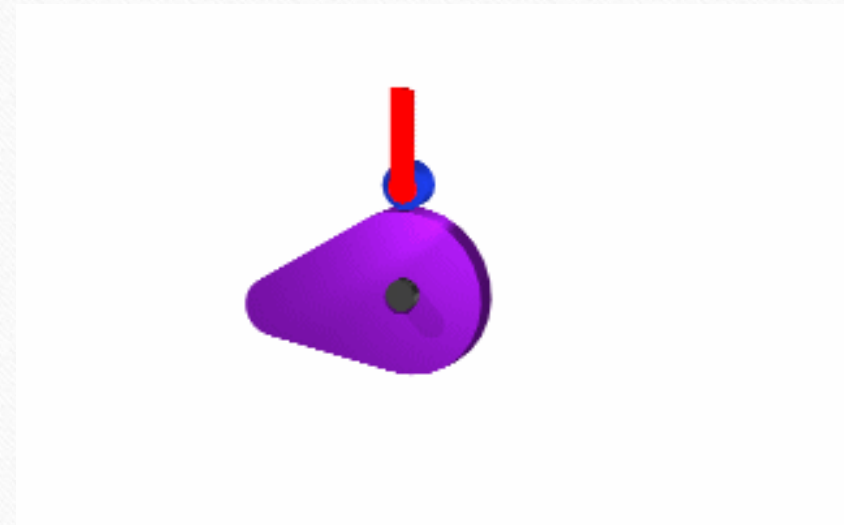
1.2.3 Translating cam – Translating follower



# Cam Mechanism

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## 1.2.1 Rotating cam – Translating follower

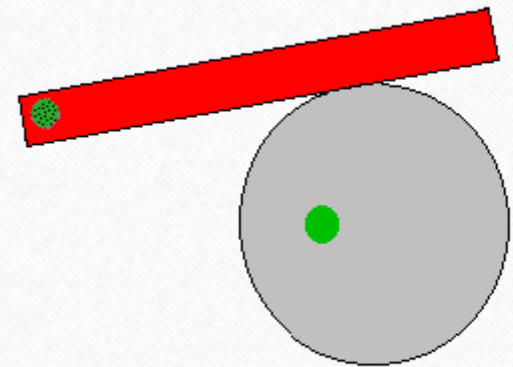




# Cam Mechanism

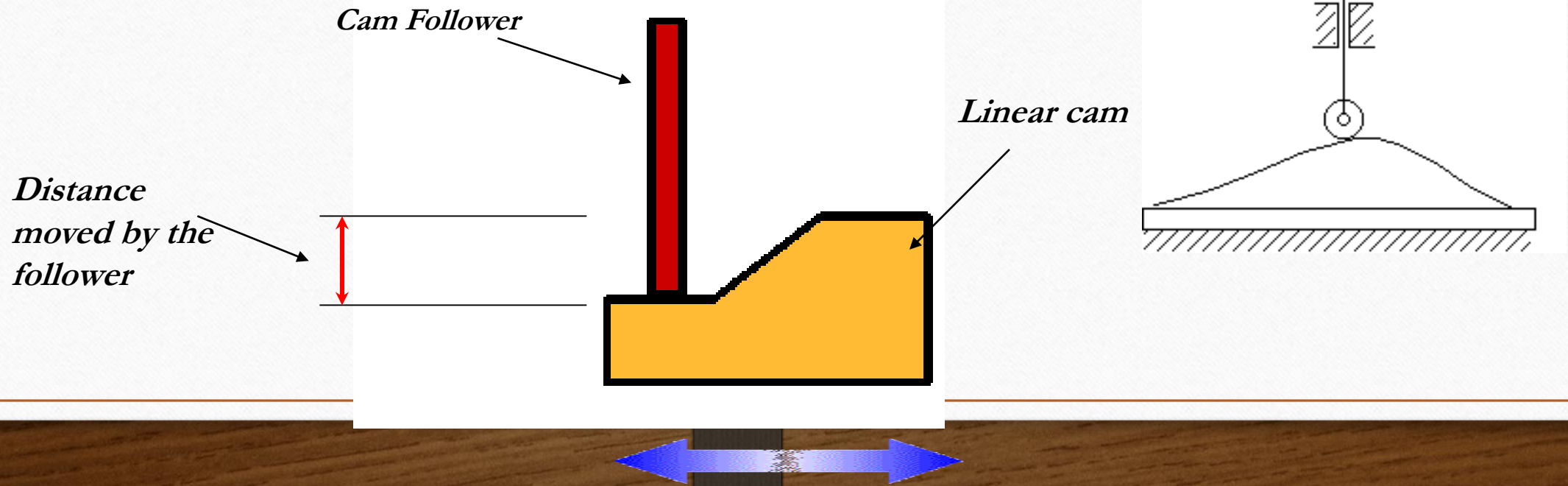
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## 1.2.2 Rotating cam – oscillating follower



# Cam Mechanism

## 1.2.3 Translating cam – Translating follower





# Followers Types

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## 1.3 Classification of followers

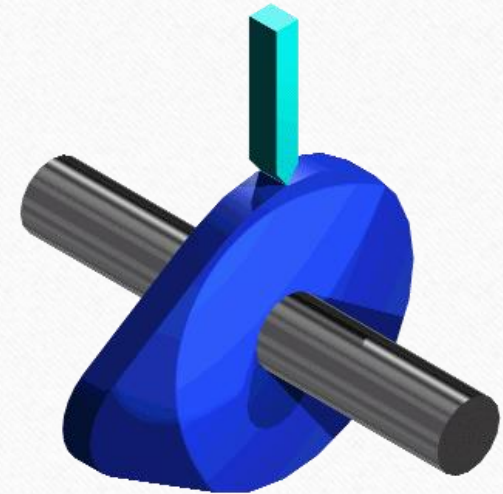
### 1.3.1 According to the shape of follower

- Knife edge follower
- Roller follower
- Flat faced follower
- Spherical faced follower

# Followers Types

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a) Knife edge follower

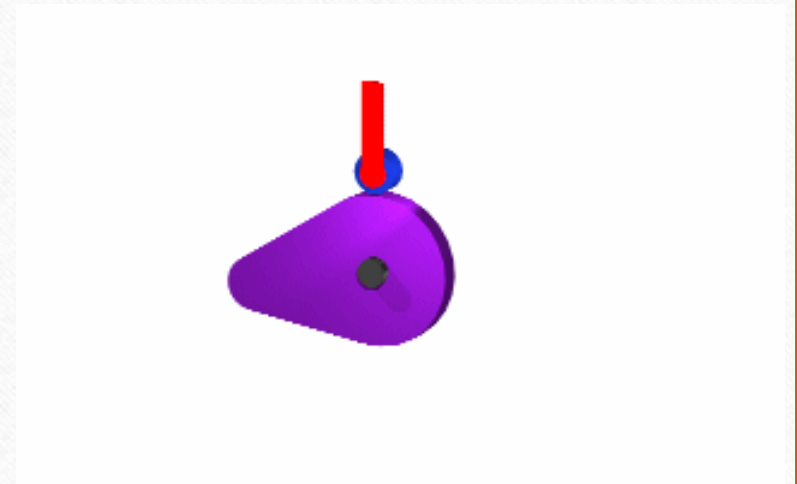




# Followers Types

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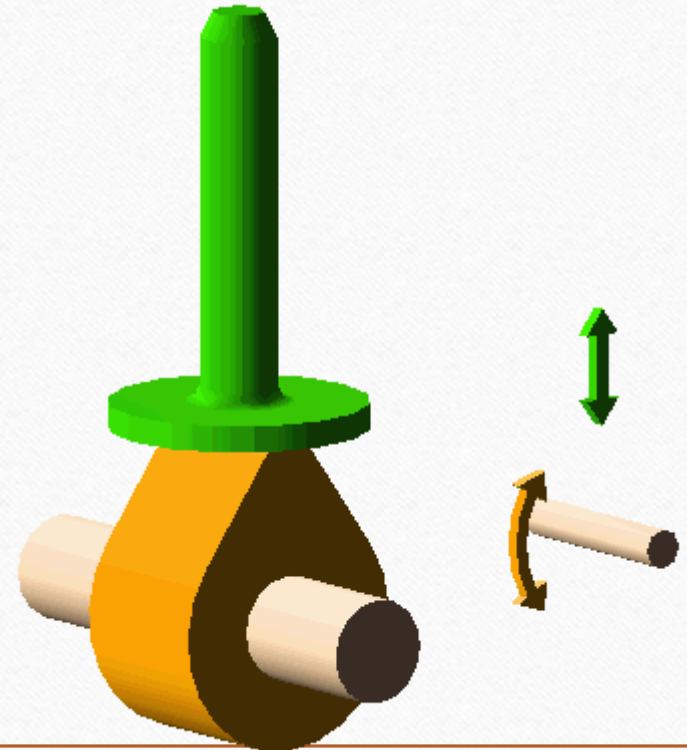
b) Roller follower



# Followers Types

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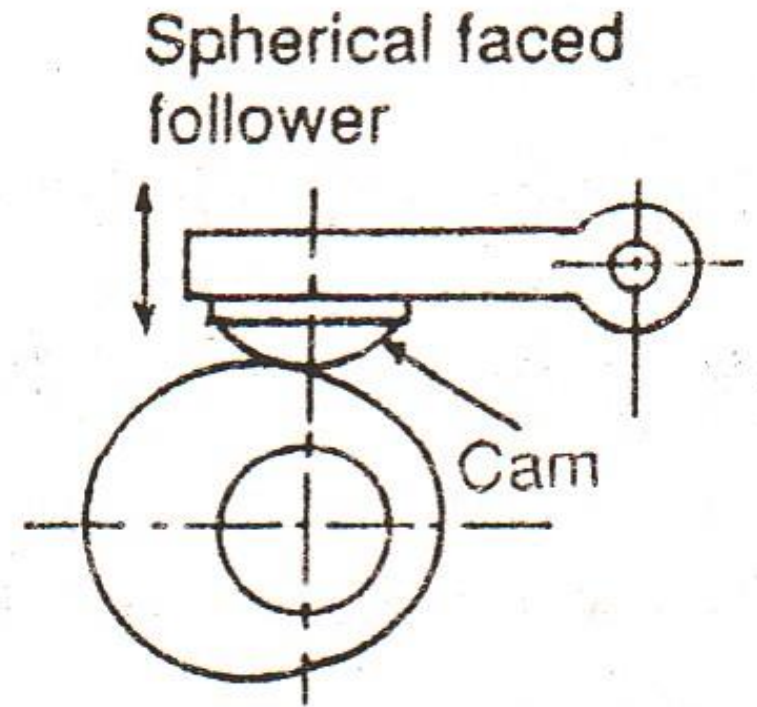
c) Flat faced follower





# Followers Types

d) Spherical faced follower

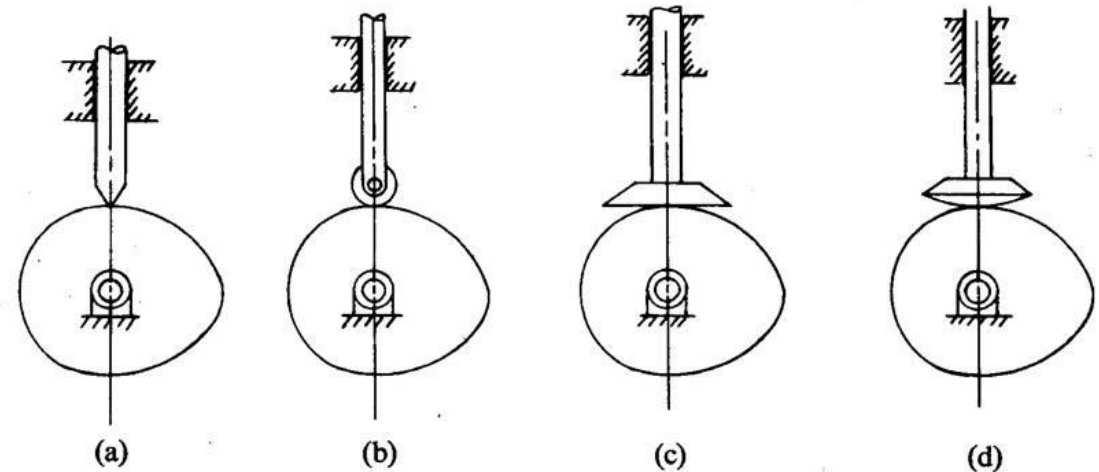


# Followers Types

## 1.3.2 According to the path of motion of follower

### a) Radial follower

- When the motion of the follower is along an axis passing through the centre of the cam, it is known as radial followers. Above figures are examples of this type.



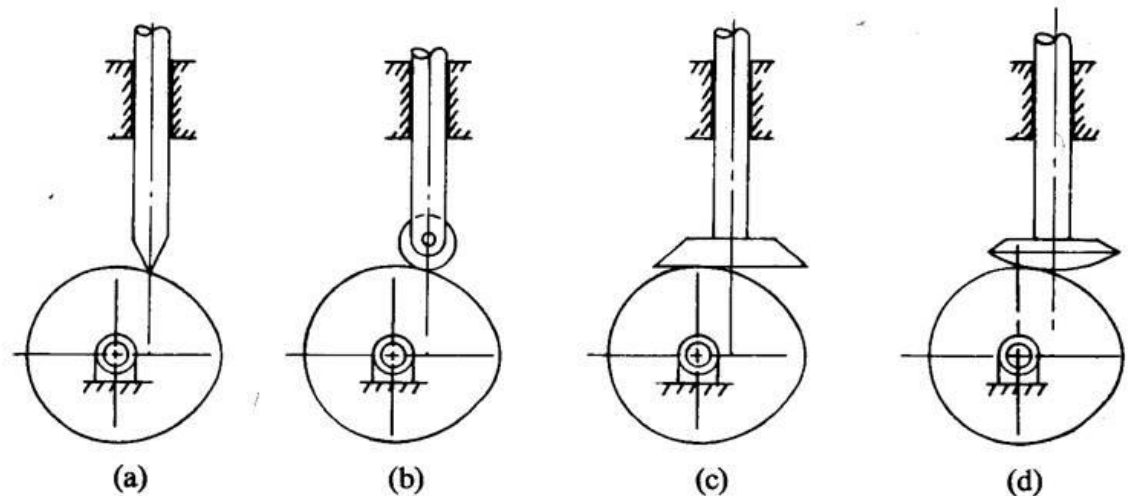


# Followers Types

## 1.3.2 According to the path of motion of follower

### b) Offset follower

When the motion of the follower is along an axis away from the axis of the cam centre, it is called off-set follower. Above figures are examples of this type.



# Cam-follower Mechanism

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## Motion Of The Follower

As the cam rotates the follower moves upward and downward.

- The upward movement of follower is called **rise (Outstroke)**
- The downward movement is called **fall (Return stroke)**.
- When the follower is not moving upward and downward even when the cam rotates, it is called **dwell**.



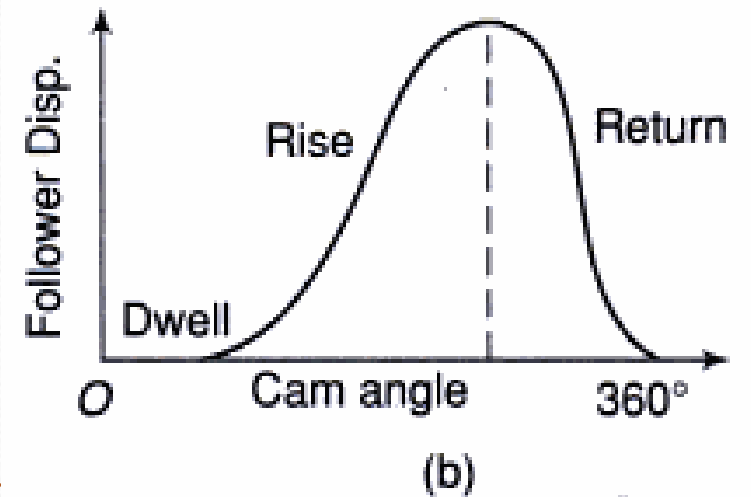
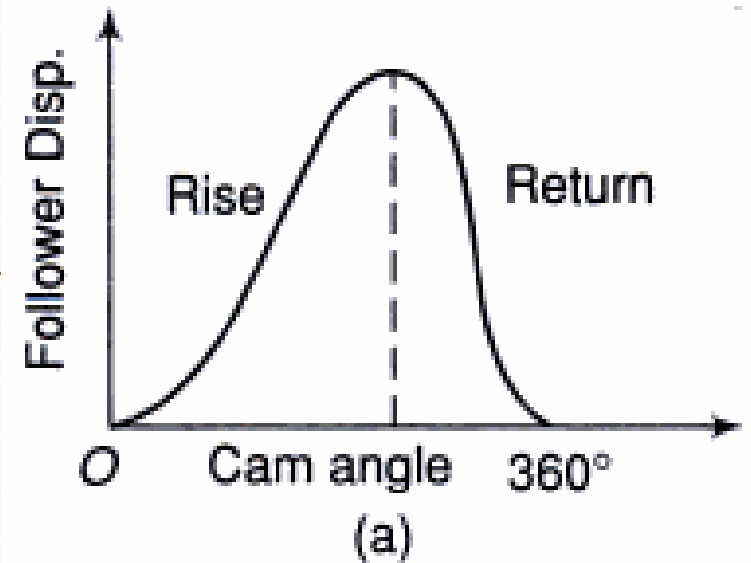
# Cam Mechanism

## 1. Rise-Return-Rise (R-R-R)

- *In this, there is alternate rise and return of the follower with no periods of dwells (Fig. a).*
- Its use is very limited in the industry.
- The follower has a linear or an angular displacement.

## 2. Dwell-Rise-Return-Dwell (D-R-R-D)

- *In such a type of cam, there is rise and return of the follower after a dwell Fig.(b).*
- *this type is used more frequently than the R-R-R type of cam.*

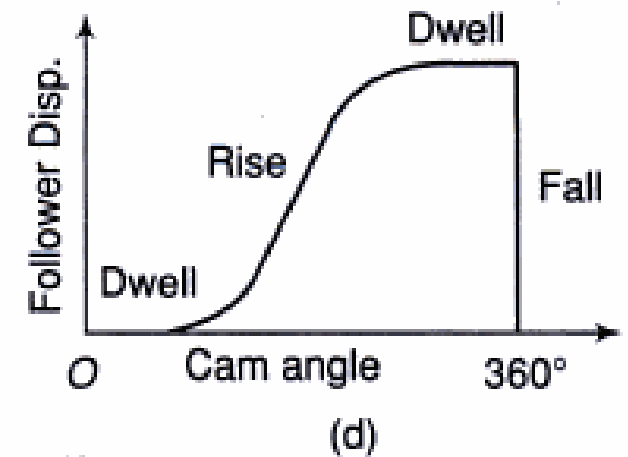
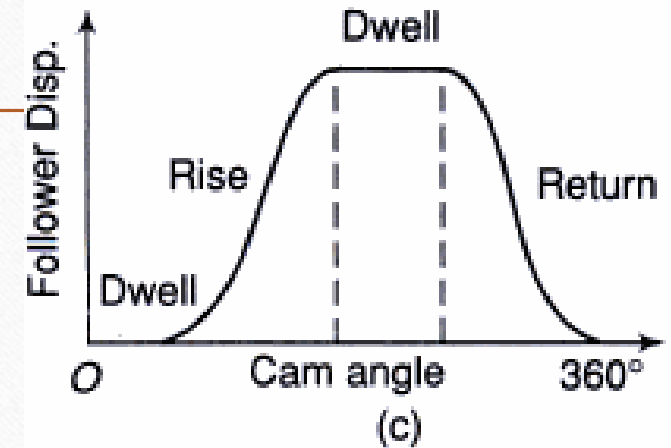


# Cam Mechanism

## 3. Dwell-Rise-Dwell-Return-Dwell (D-R-D-R-D)

It is the most widely used type of cam.

- *The dwelling of the cam is followed by rise and dwell and subsequently by return and dwell as shown in rig. (c).*
- In case the return of the follower is by a fall [Fig.(d)], the motion may be known as Dwell-Rise-Dwell (D-R-D).

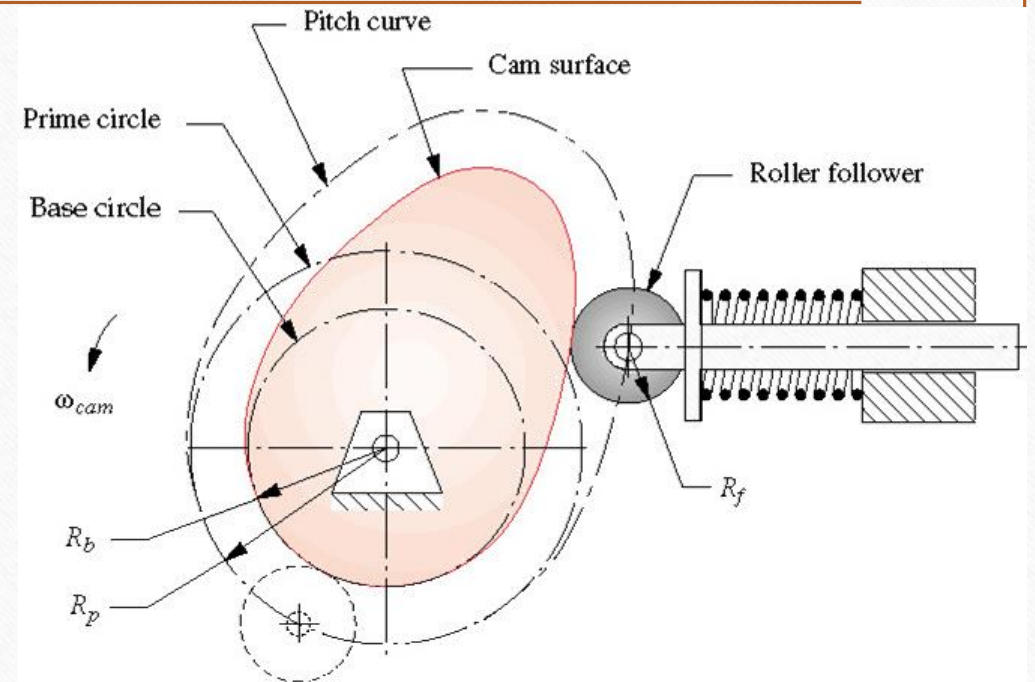




# Graphical layout of cam profiles

## Terminology

- **Cam profile:** The outer surface of the disc cam.
- **Base circle :** The circle with the shortest radius from the cam center to any part of the cam profile.
- **Trace point:** It is a point on the follower, and its motion describes the movement of the follower. It is used to generate the pitch curve.

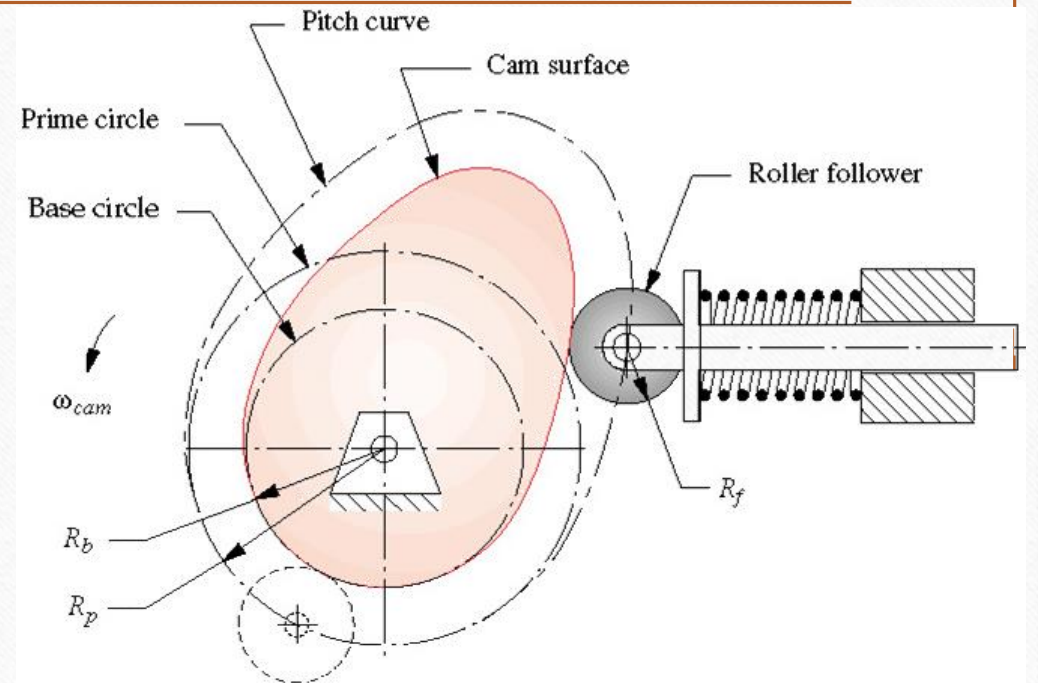




# Graphical layout of cam profiles

## Terminology

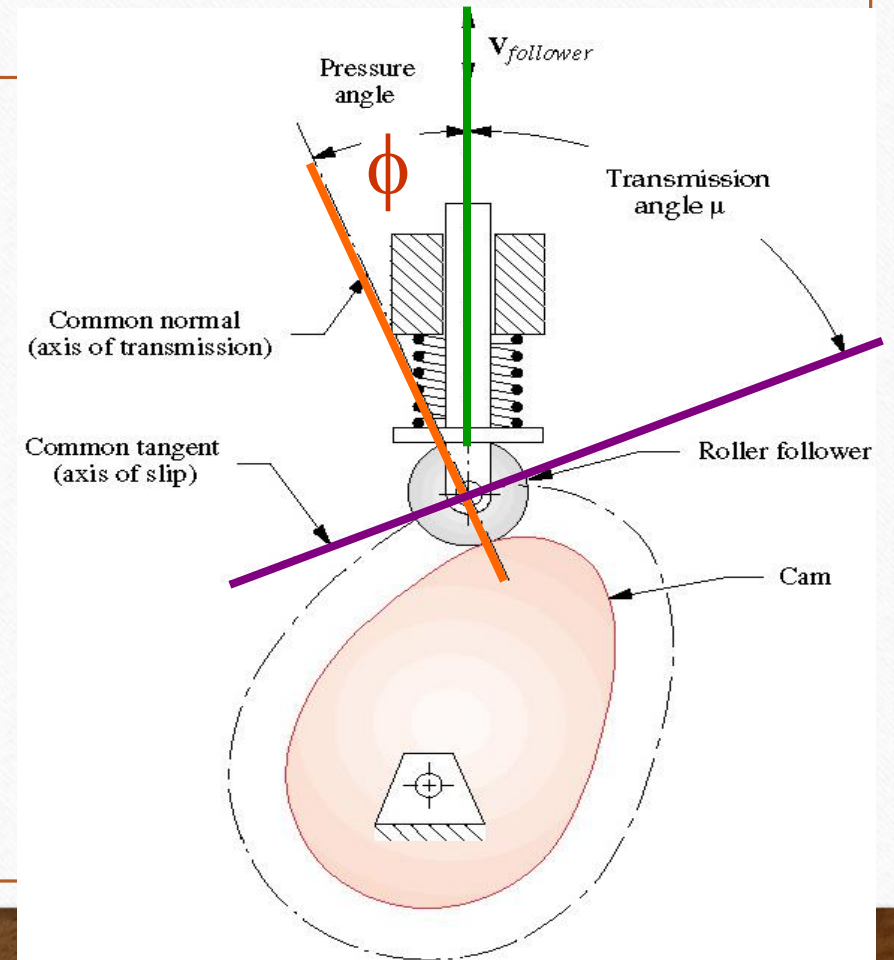
- **Pitch curve** : The path generated by the trace point as the follower is rotated about a stationery cam.
- **Prime circle**: The smallest circle from the cam center through the pitch curve



# Graphical layout of cam profiles

## Terminology

- **Pressure angle:** The angle between the direction of the follower movement and the normal to the pitch curve.
- **Pitch point:** Pitch point corresponds to the point of maximum pressure angle.
- **Pitch circle:** A circle drawn from the cam center and passes through the pitch point is called Pitch circle
- **Stroke:** The greatest distance or angle through which the follower moves or rotates

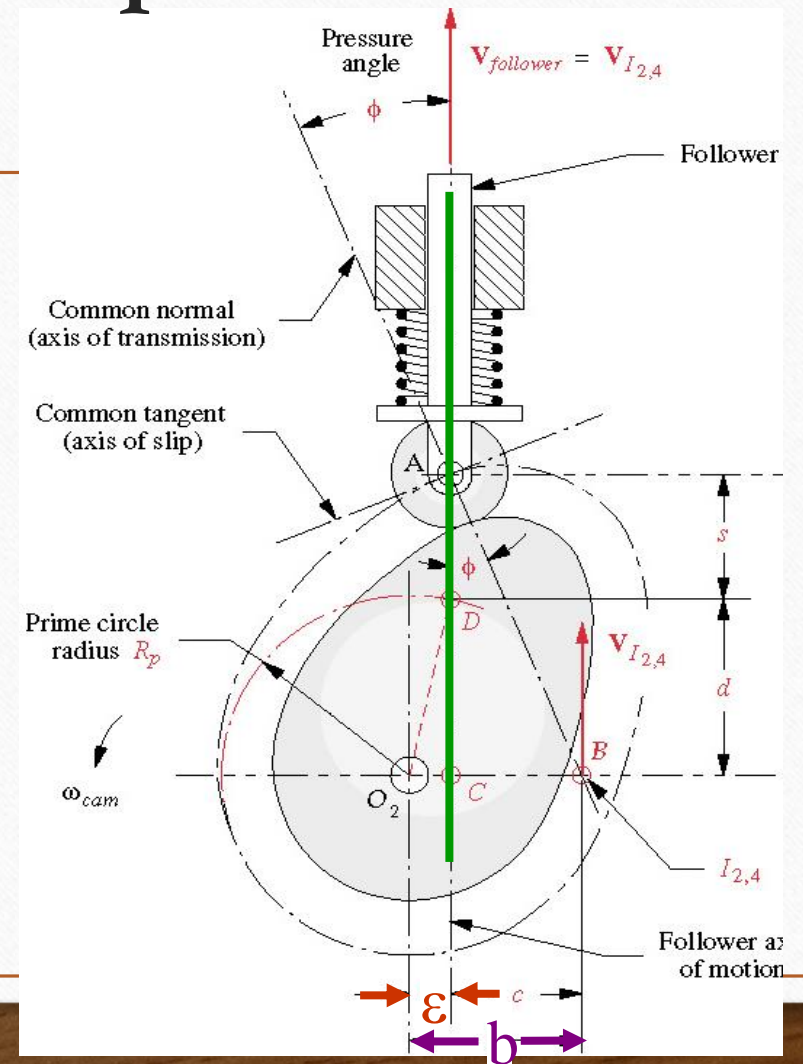




# Graphical layout of cam profiles

## Cam Eccentricity

- Eccentricity ( $\epsilon$ ) – the perpendicular distance between the follower's axis of motion and the center of the cam
- Aligned follower:  $\epsilon=0$





# Cam Profile

## Types of follower motion

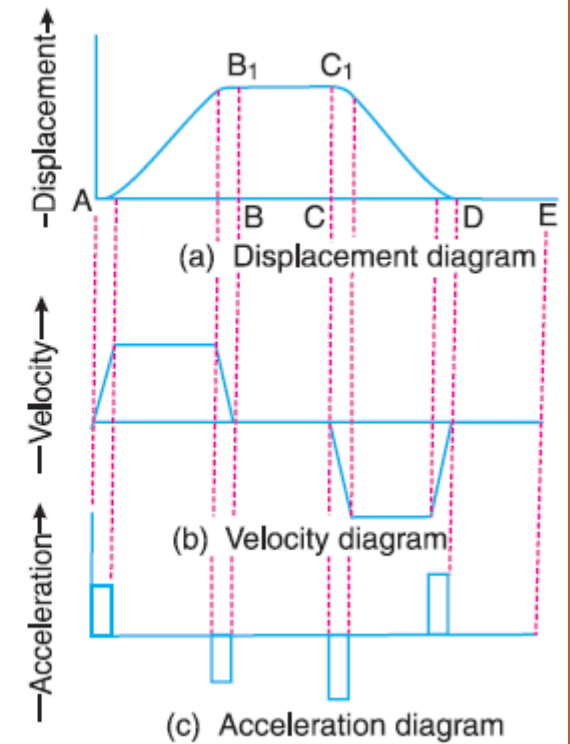
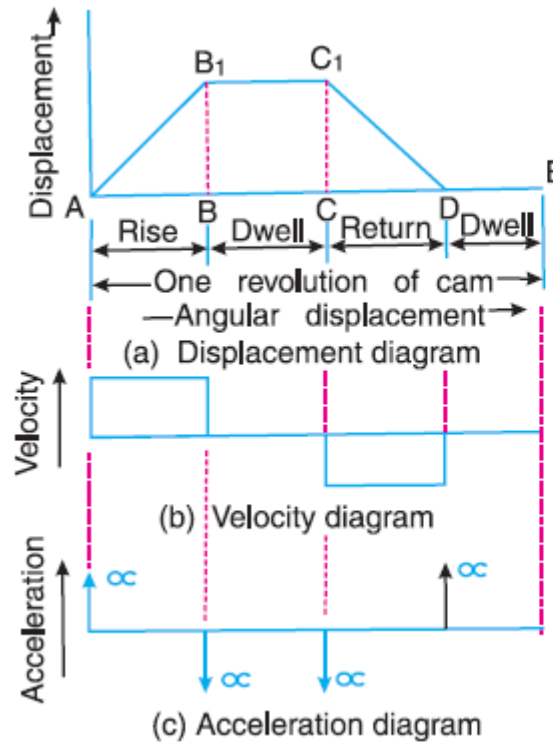
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1. Uniform motion ( constant velocity)
  - Constant velocity
  - Problem: infinity acceleration at point where dwell portion starts
2. Simple harmonic motion (Sinusoidal )
3. Uniform acceleration and retardation motion
  - Can be shown that acceleration is constant
4. Cycloidal motion

# Cam Profile

## a) Uniform motion (constant velocity)

- **Displacement diagram:** Displacement is the distance that a follower moves during one complete revolution (or cycle) of the cam while the follower is in contact with the cam.
- It is the plot of linear displacement (s) of follower V/S angular displacement ( $\theta$ ) of the cam for one full rotation of the cam.

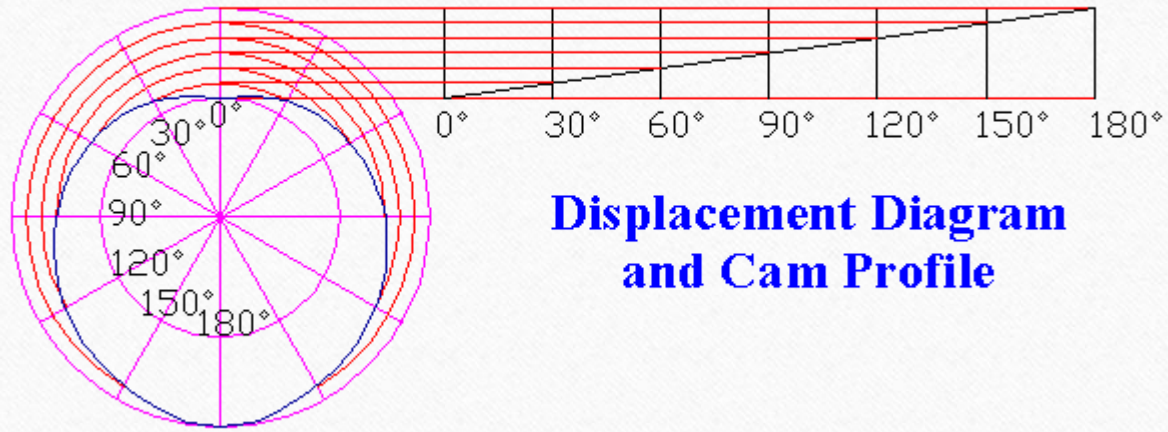




# Cam Profile

a) Uniform motion (constant velocity)

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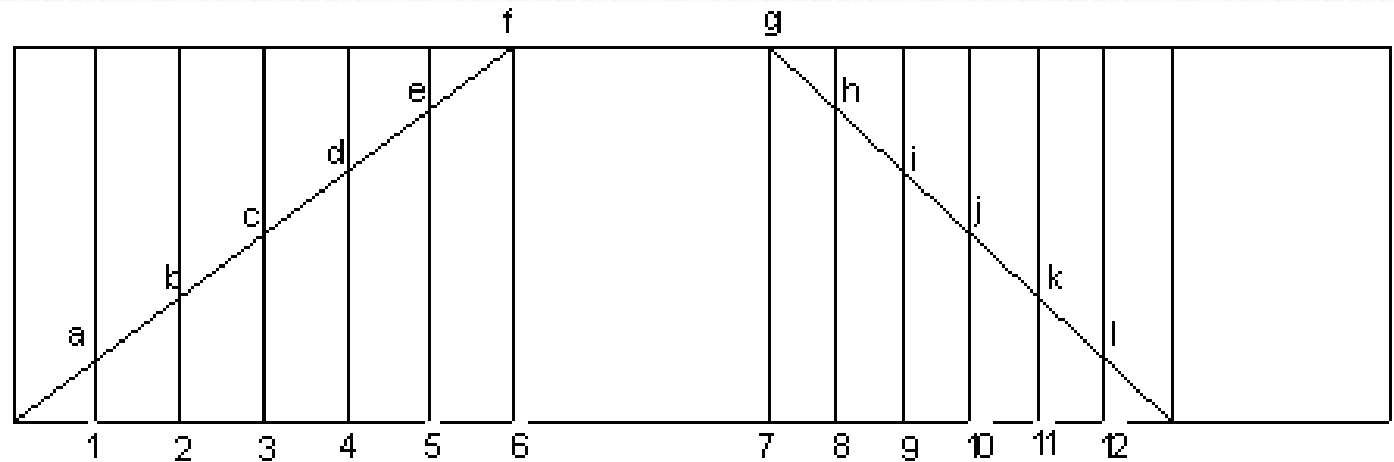


# Cam Profile

## a) Uniform motion (constant velocity)

### Displacement diagram

Since the follower moves with uniform velocity during its rise and fall, the slope of the displacement curve must be constant as shown in fig



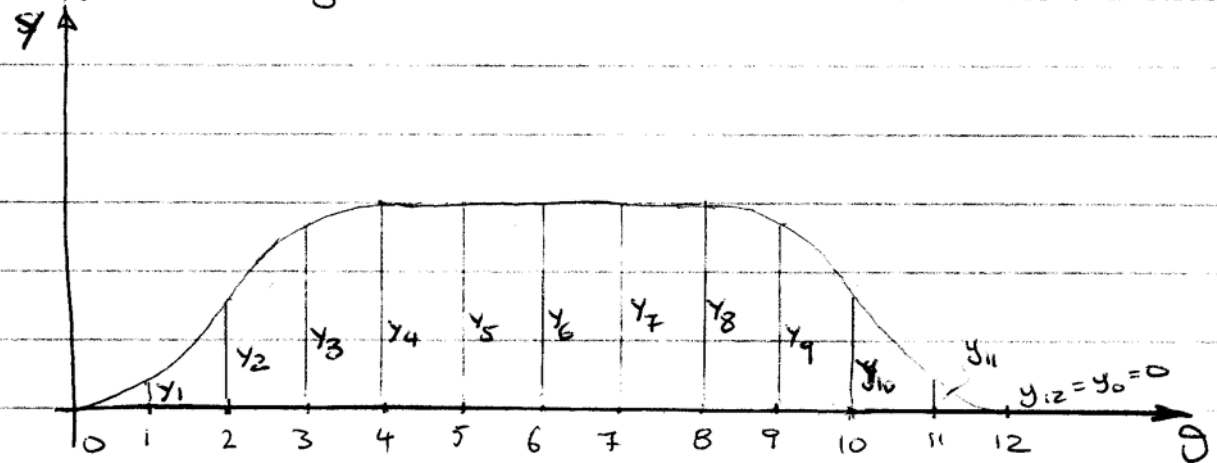
# Constructing cam profile: kinematic inversion principle

## Steps:

- Break range of  $\theta$  in 12 positions
- Measure displacement of follower at each point,  $y_1, y_2$
- Define base circle of cam
- Divide base circle to 12 equal sectors
- Mark 12 radials in opposite direction of cam rotation
- Mark follower displacements on radials
- Sketch cam

Finding cam shape given the displacement diagram:

knife-edge translating follower

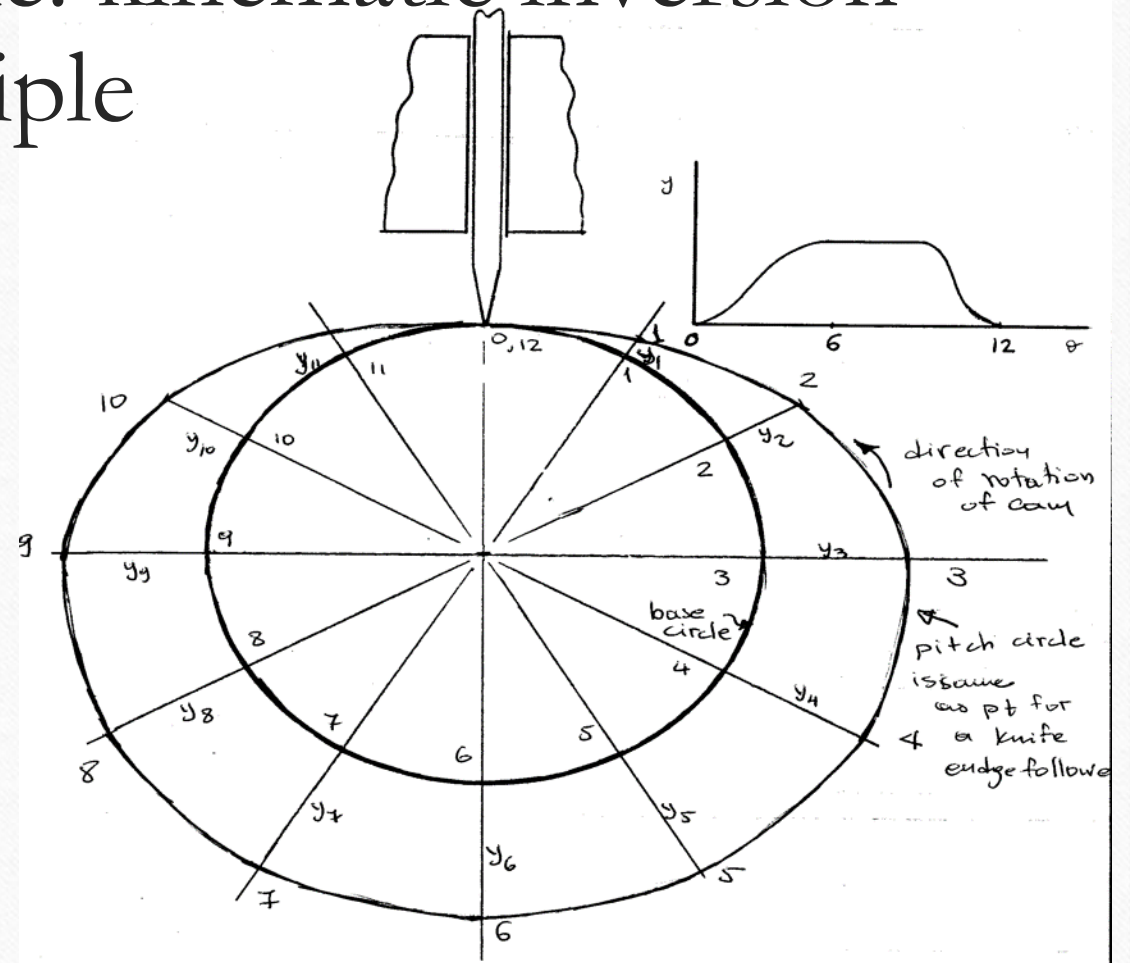




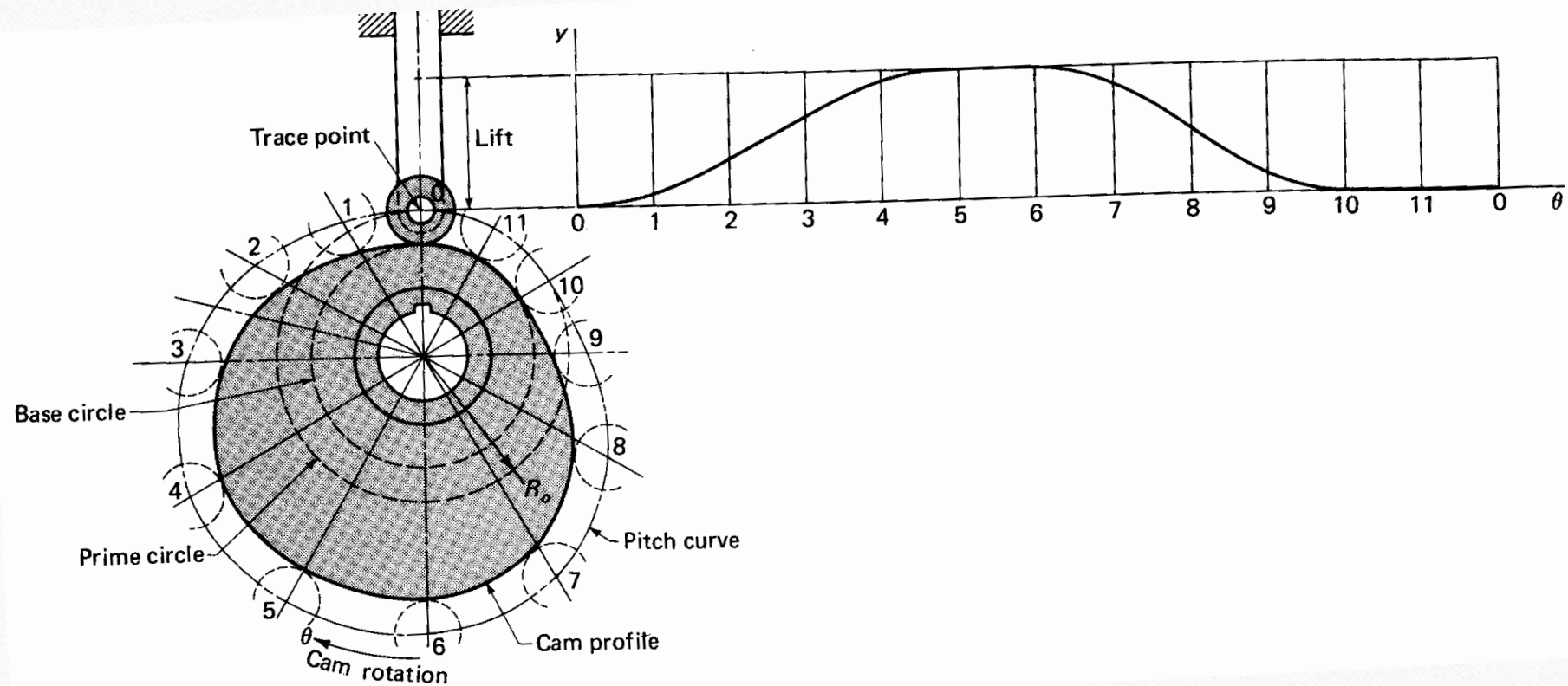
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# Layout of cam profile: roller follower

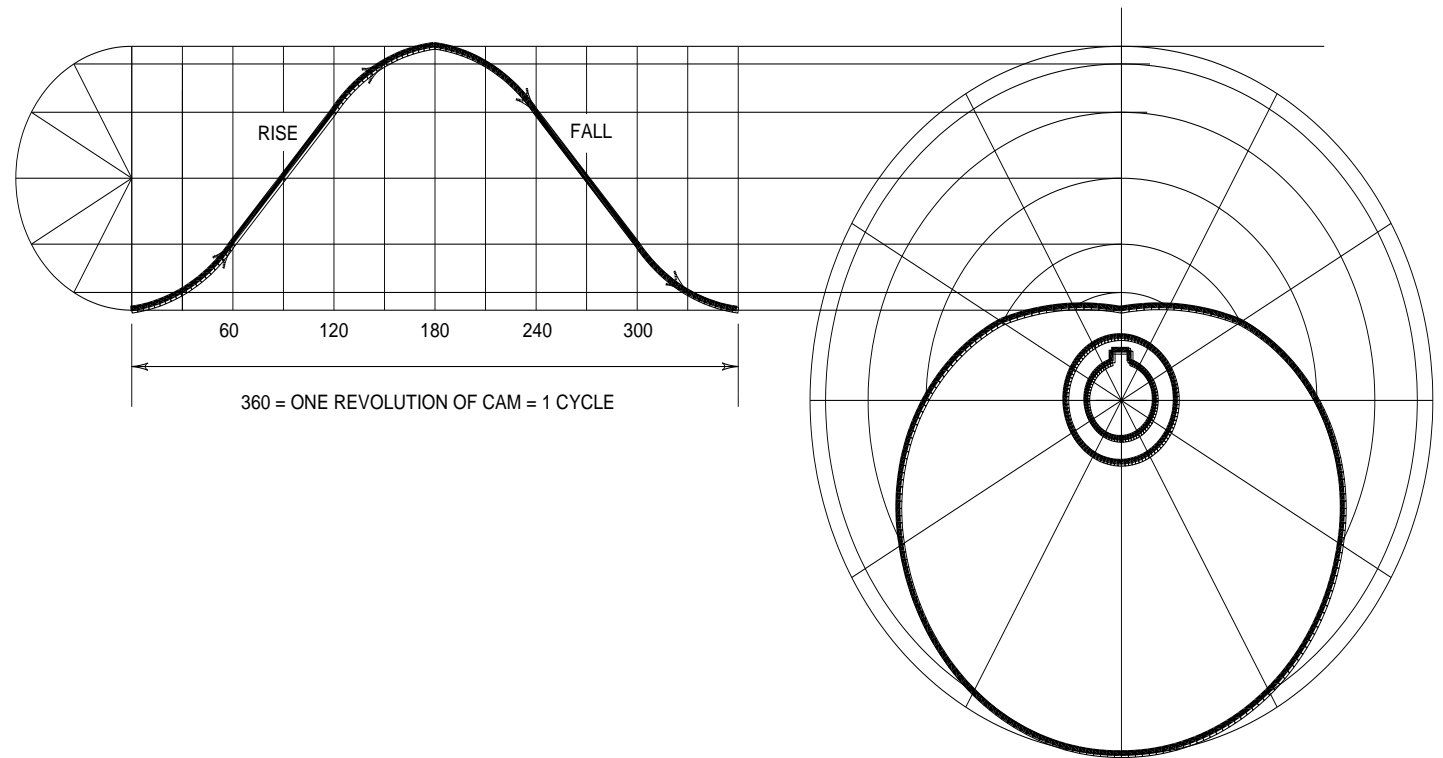




# Cam Profile

## b) Simple Harmonic motion

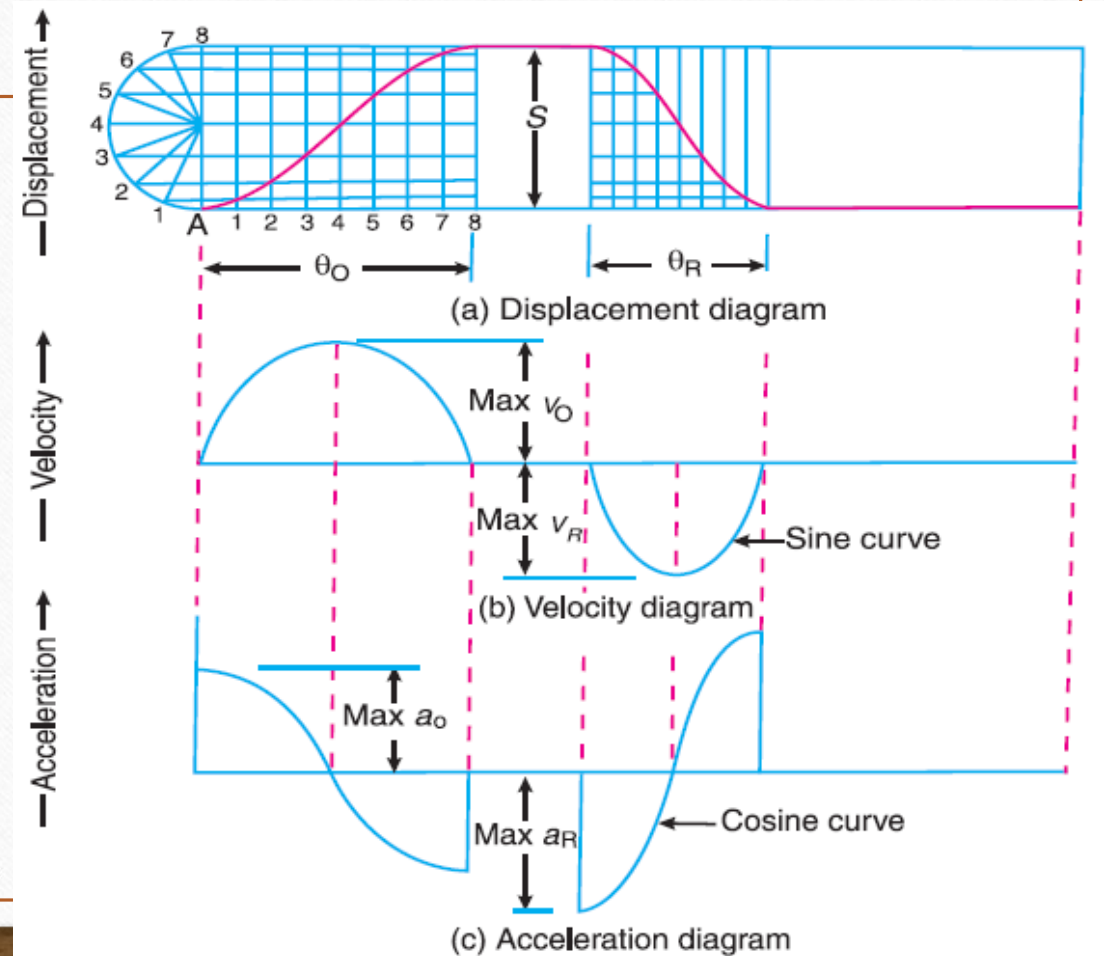
- Since the follower moves with a simple harmonic motion, therefore velocity diagram consists of a sine curve and the acceleration diagram consists of a cosine curve.



# Cam Profile

## b) Simple Harmonic motion

- Since the follower moves with a simple harmonic motion, therefore velocity diagram consists of a sine curve and the acceleration diagram consists of a cosine curve.





# Cam Profile

## b) Simple Harmonic motion

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Let  $S$  = Stroke of the follower,

$\theta_O$  and  $\theta_R$  = Angular displacement of the cam during out stroke and return stroke of the follower respectively, in radians, and

$\omega$  = Angular velocity of the cam in rad/s.

maximum velocity of the follower on the outstroke,  $\frac{\pi\omega S}{2\theta_O}$

$\therefore$  Maximum acceleration of the follower on the outstroke,

$$a_O = a_P = \frac{\pi^2 \omega^2 \cdot S}{2(\theta_O)^2}$$

Similarly, maximum velocity of the follower on the return stroke,

$$v_R = \frac{\pi\omega S}{2\theta_R}$$

and maximum acceleration of the follower on the return stroke,

$$a_R = \frac{\pi^2 \omega^2 \cdot S}{2(\theta_R)^2}$$

# Cam Profile

## c) Uniform acceleration and retardation

- Since the acceleration and retardation are uniform, therefore the velocity varies directly with time.

velocity of the follower during outstroke,

$$v_O = \frac{2\omega S}{\theta_O}$$

maximum velocity of the follower during return

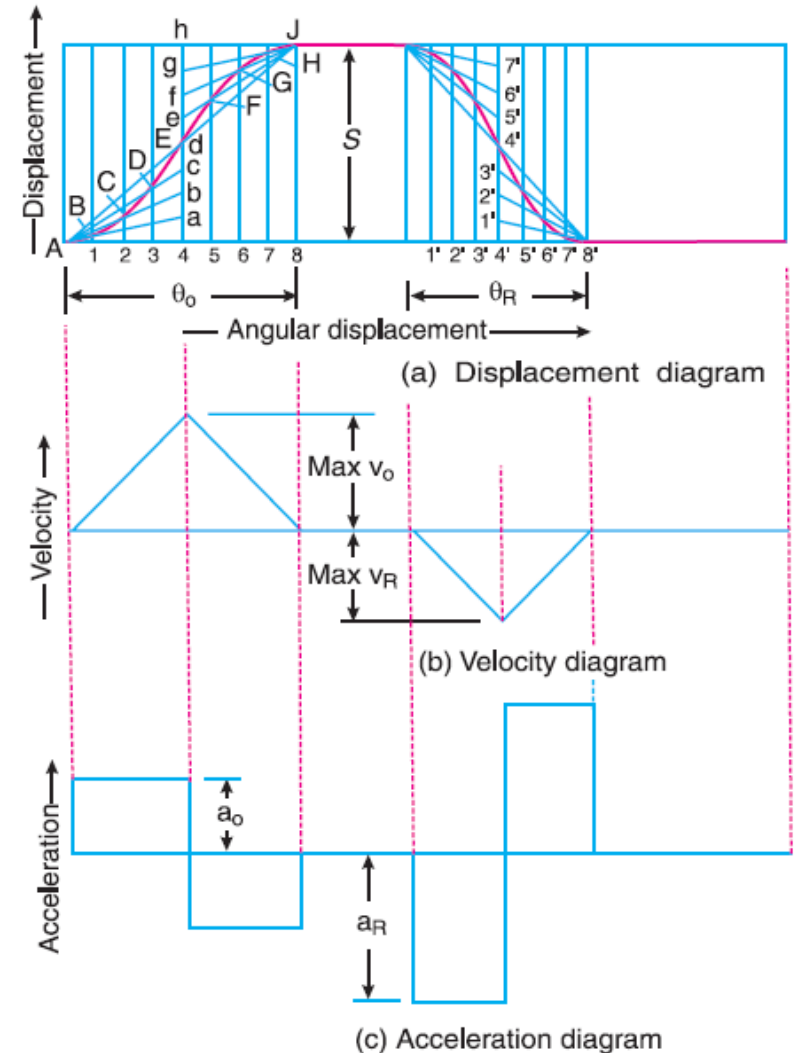
$$v_R = \frac{2\omega S}{\theta_R}$$

Maximum acceleration of the follower during outstroke,

$$a_O = \frac{4\omega^2 \cdot S}{(\theta_O)^2}$$

Similarly, maximum acceleration of the follower during return

$$a_R = \frac{4\omega^2 \cdot S}{(\theta_R)^2}$$





# Cam Profile

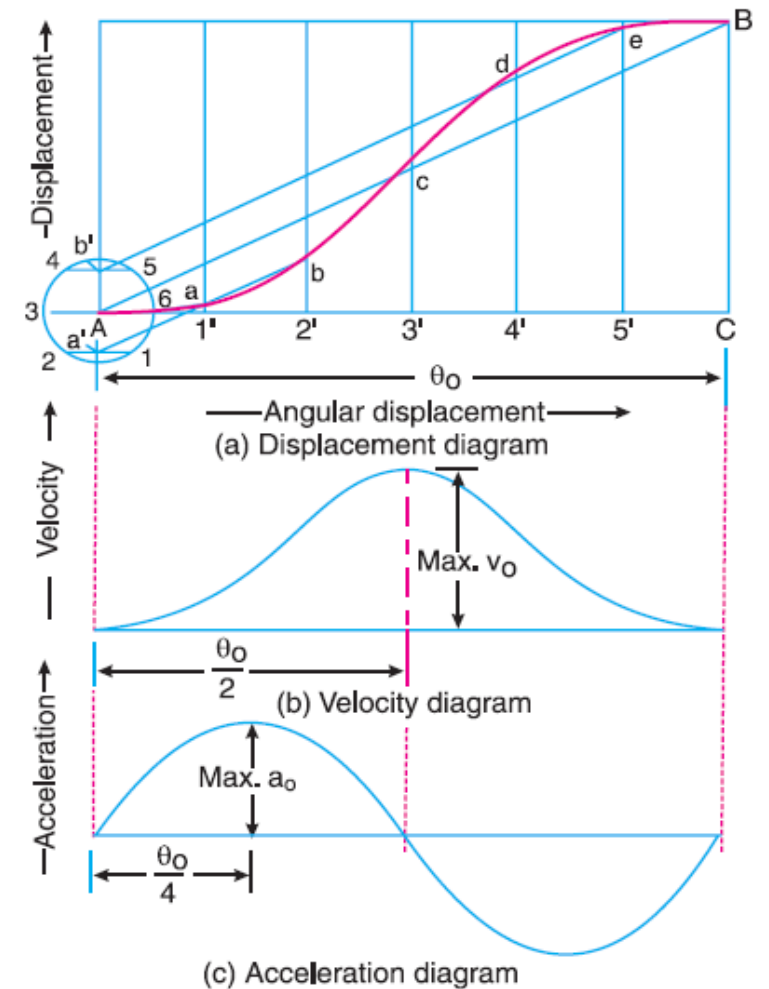
## d) Cycloidal motion

$$v_O = \frac{2\omega S}{\theta_O}$$

$$a_O = \frac{2\pi\omega^2.S}{(\theta_O)^2}$$

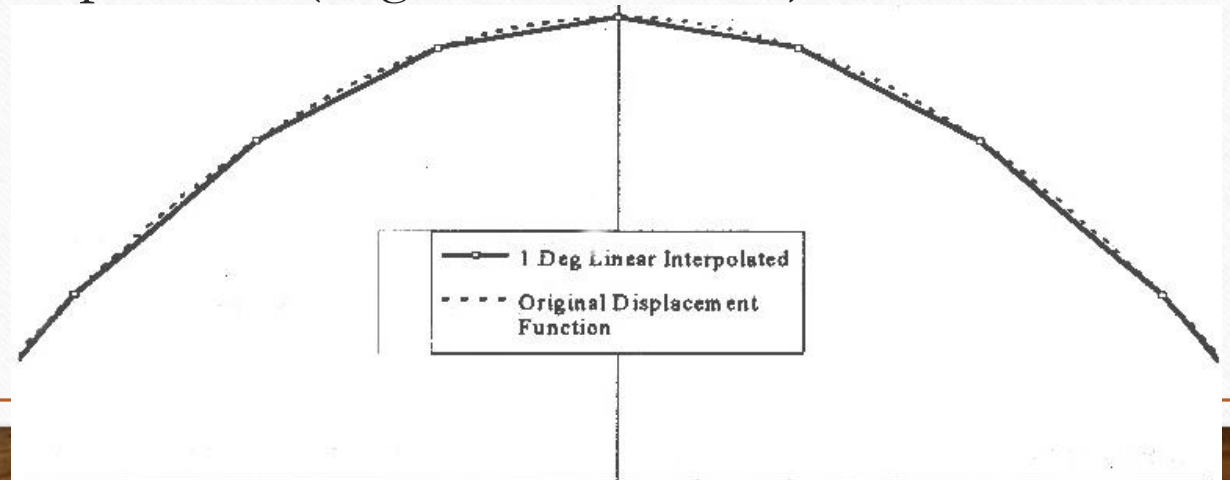
$$v_R = \frac{2\omega.S}{\theta_R}$$

$$a_R = \frac{2\pi\omega^2.S}{(\theta_R)^2}$$



# Cam Manufacturing Considerations

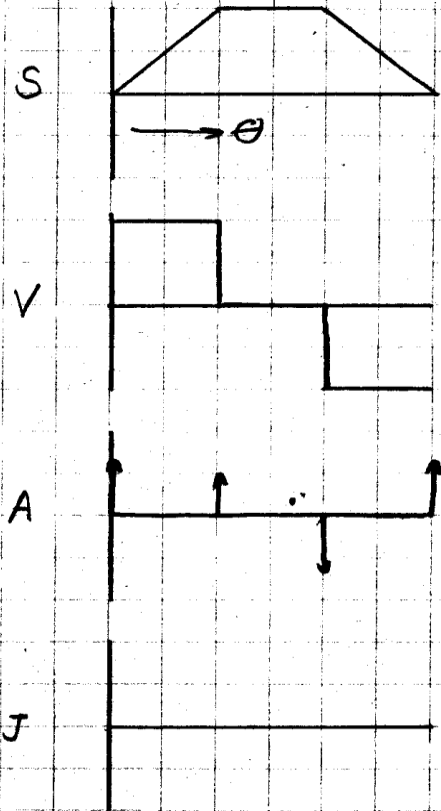
- Medium to high carbon steels, or cast ductile iron
- Milled or ground
- Heat treated for hardness (Rockwell HRC 50-55)
- CNC machines often use linear interpolation (larger accelerations)





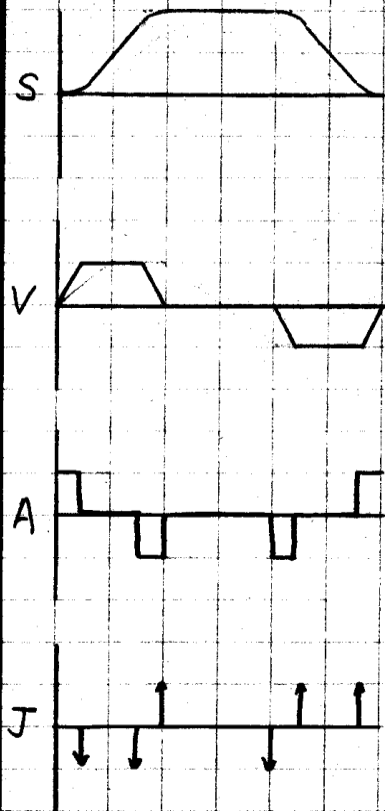
SVAJ diagrams: show displacement, velocity, acceleration versus  $\theta$

CV



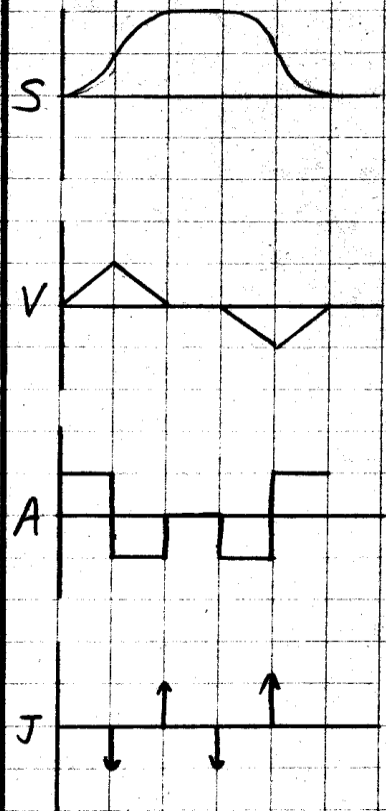
Accel =  $\infty \rightarrow \infty$  inertia forces, separation, wear.

MCV



gets rid of inf. accel but Jerk =  $\infty \rightarrow$  bad vibes

CA



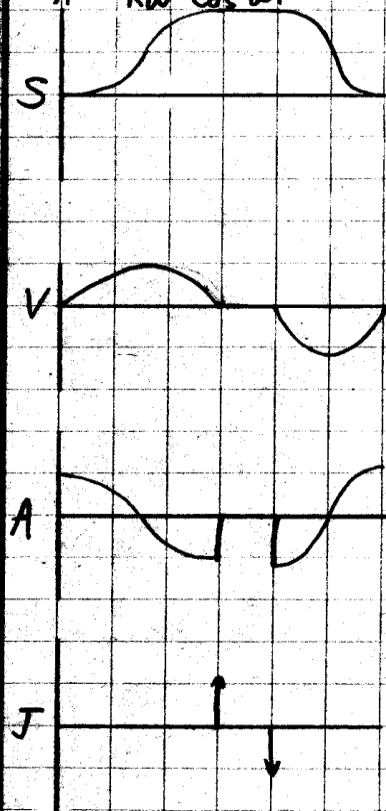
(Jerk is  $\infty$ , thus bad) vibes

SHM

$$S = R(1 - \cos \omega t)$$

$$V = R\omega \sin \omega t$$

$$A = R\omega^2 \cos \omega t$$

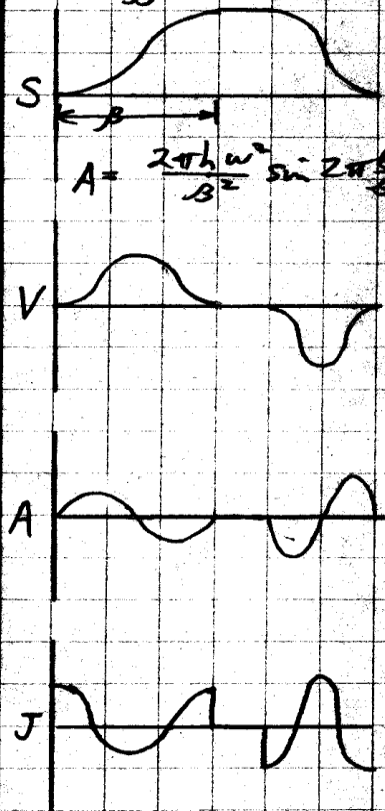


If no dwell  $\rightarrow$  no infinite jerks

CYC.

$$S = \frac{h}{2\pi} \left( 2\pi \frac{\theta}{\beta} - \sin 2\pi \frac{\theta}{\beta} \right)$$

$$V = \frac{h\omega}{\beta} \left( 1 - \cos 2\pi \frac{\theta}{\beta} \right)$$



no inf. jerks but for a given h in a given  $\theta$ , you have the highest accel.